Study of Z boson production in pPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV

The CMS Collaboration

Abstract

The production of Z bosons in pPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV is studied by the CMS experiment via the electron and muon decay channels. The inclusive cross section is compared to pp collision predictions, and found to scale with the number of elementary nucleon-nucleon collisions. The differential cross sections as a function of the Z boson rapidity and transverse momentum are measured. Though they are found to be consistent within uncertainty with theoretical predictions both with and without nuclear effects, the forward-backward asymmetry suggests the presence of nuclear effects at large rapidities. These results provide new data for constraining nuclear parton distribution functions.

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1 Introduction

Electroweak boson production is an important benchmark process in high-energy particle physics. The production of Z and W bosons has been extensively studied at hadron and $e^+e^-$ colliders, at various collision energies. The latest measurements in pp collisions at the LHC [1–8] are well described by the standard model using higher-order perturbative quantum chromodynamics (QCD) and parton distribution functions (PDFs).

With its large center-of-mass energy and high luminosity, the LHC enables for the first time the study of Z and W boson production in heavy ion collisions. Electroweak bosons are unmodified by the hot and dense medium created in nucleus-nucleus collisions, and their leptonic decays are of particular interest since leptons pass through the medium without being affected by the strong interaction. Both the Z and W boson production were measured by the ATLAS [9, 10] and the CMS [11, 12] experiments using PbPb collisions taken in 2010 and 2011 at a center-of-mass energy per nucleon pair of $\sqrt{s_{NN}} = 2.76$ TeV, confirming that the production cross section scales with the number of elementary nucleon-nucleon collisions with a precision of about 10%.

However, in nuclear collisions, the production of electroweak bosons can be affected by the initial conditions of the collision. The free-proton PDFs are expected to be modified for protons bound in the Pb nucleus, which, together with the fact that the nucleus contains neutrons as well as protons (isospin effect), can modify the observed cross sections as compared to pp collisions. Various groups have studied the nuclear modification of PDFs, and several results are available at next-to-leading-order (NLO) precision in QCD [13–15]. These results are obtained by global fits to the available deep inelastic scattering and Drell–Yan data, which constrain the nuclear PDFs (nPDFs) in the region of parton longitudinal momentum fraction $x > 10^{-2}$ and four-momentum transfer squared $Q^2 < (10 \text{ GeV})^2$.

The production of electroweak bosons in proton-nucleus collisions at the LHC provides an opportunity to study the nPDFs at the high $Q^2 \approx (100 \text{ GeV})^2$ and lower $x$ phase space region [16]. The CMS experiment made the first measurement of W boson production in pPb collisions [17]. Deviations from the current expectations for PDFs were observed, showing the need for including W boson data in nPDF global fits. Furthermore, the dijet pseudorapidity distribution measured in pPb collisions by CMS [18] and the Z boson production in pPb collisions measured by ATLAS [19] show better agreement with modified PDFs. Deviations from pp expectations were also seen with charged hadrons [20].

Various models predict different nuclear modifications of the Z boson production cross section ($\sigma$) as a function of transverse momentum ($p_T$) and rapidity in the nucleon-nucleon center-of-mass frame ($y_{cm}$) [21–25]. Processes mediated by a virtual photon and interference effects are also considered as part of the Z boson signal. The rapidity distribution of Z bosons is particularly sensitive to the parton content of the interacting nucleons. Consequently, the symmetric rapidity spectrum of the Z bosons in the center-of-mass frame of pp collisions is modified by nuclear effects in pPb collisions [24]. This can be quantified through measurements of the forward-backward asymmetry in the center-of-mass frame:

$$R_{FB}(y_{cm}) = \frac{d\sigma(+y_{cm})/dy_{cm}}{d\sigma(-y_{cm})/dy_{cm}},$$

where by convention positive rapidity values correspond to the direction of the incoming proton.

The aim of this paper is to study the $Z \rightarrow \ell\ell$ process (where $\ell$ represents either muons or electrons) and to measure the production cross section as functions of rapidity and transverse
momentum. The typical quark momentum fraction probed in the Pb nucleus is given by \( x = M_Z / \sqrt{s_{NN}} - y_{cm} \), and thus with 0.002 < x < 0.3 in the measured range of \(-2.8 < y_{cm} < 2.0\). These measurements will help to constrain the parton content of the nucleons in the nucleus.

2 Experimental setup, data selection and reconstruction

A detailed description of the CMS detector and its coordinate system can be found elsewhere [26]. Its central feature is a superconducting solenoid with internal diameter of 6 m, providing a magnetic field of 3.8 T. Within the solenoid volume are a silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass and scintillator hadron calorimeter (HCAL). Muons are detected in the pseudorapidity range \(|\eta_{\text{lab}}| < 2.4\) using gas-ionization detectors embedded in the steel return yoke outside the solenoid. Electrons are measured in the ECAL that consists of 75,848 lead tungstate crystals providing a coverage in the barrel region of \(|\eta_{\text{lab}}| < 1.48\) and in the two endcap regions of 1.48 < \(|\eta_{\text{lab}}| < 3.00\). Extensive forward calorimetry complements the coverage provided by these barrel and endcap detectors. CMS has a two-level trigger system. The first level, composed of custom hardware processors, uses information from the calorimeters and muon detectors to select the most interesting events. The high-level trigger processor farm further decreases the event rate before data storage.

The analysis is performed using the pPb collision data taken at the beginning of 2013 and corresponding to an integrated luminosity of 34.6 ± 1.2 nb\(^{-1}\) [27]. The beam energies were 4 TeV for protons and 1.58 TeV per nucleon for lead nuclei, resulting in a center-of-mass energy per nucleon pair of \( \sqrt{s_{NN}} = 5.02 \) TeV. As a consequence of the energy difference between the colliding beams, the nucleon-nucleon center-of-mass frame is not at rest with respect to the laboratory frame. Massless particles emitted at rapidity \( y_{cm} = 0 \) in the nucleon-nucleon center-of-mass frame will be detected at \( y_{\text{lab}} = -0.465 \) (clockwise proton beam) or +0.465 (counterclockwise proton beam) in the laboratory frame. The results presented here are expressed in the center-of-mass frame with the proton-going side defining the region of positive \( y_{cm} \) values, to respect the usual convention of the proton fragmentation region being probed at positive rapidity. The direction of the higher energy proton beam was initially clockwise and was then reversed, producing two comparable datasets.

During data taking, muon and electron triggers were employed to select and record all events with high-\( p_T \) leptons. The measurements in the muon final state are based on a sample obtained by requiring at least one muon with \( p_T \) greater than 12 GeV/c. The muon candidates are reconstructed with an algorithm that combines information from both the silicon tracker and the muon system [28]. Background muons from cosmic rays and heavy-quark semileptonic decays are rejected by applying a set of quality criteria to each muon, based on previous studies of the performance of the muon reconstruction [28]. The muons are selected by requiring at least two muon stations to be matched to the muon track, a low \( \chi^2/\text{ndf} \) of the global fit, a minimum number of tracker layers and pixel hits, and finally, a maximum distance from the primary vertex in the transverse and longitudinal direction.

The electron measurements are based on a candidate photon or electron sample collected by requiring at least one ECAL transverse energy deposit of \( E_T > 15 \) GeV and online identification criteria that are looser than the electron selection applied offline. Electrons are reconstructed by matching ECAL clusters to tracks measured in the silicon tracker. This matching is used to differentiate electrons from photons [29]. The identification criteria are chosen to match those used for pp collisions [30]. The electrons are selected by requiring a match between the \( \eta \) and \( \phi \)
coordinates of the track and the ECAL cluster, a narrow width of the ECAL cluster in $\eta$, a low HCAL energy measured in the ECAL cluster direction and by rejecting electrons with a partner track consistent with a photon conversion. In this measurement, no isolation requirements are imposed on the leptons.

3 Analysis procedure

The $Z$ boson production cross section is calculated using the following equation:

$$\sigma = \frac{S - B}{\alpha \epsilon L_{\text{int}}},$$

where $S$ is the number of $Z$ candidates, $B$ is the estimated background, $\alpha$ is the acceptance, $\epsilon$ is the efficiency, including correction factors derived from data, and $L_{\text{int}}$ is the integrated luminosity. The phase space region considered in the analysis is defined by requiring two leptons with $p_T > 20\text{ GeV/c}$ and with pseudorapidity in the laboratory frame $|\eta_{\text{lab}}| < 2.4$ in order to ensure that the triggers are maximally efficient and are within the geometrical coverage of the muon detectors. This fiducial region of the measurement is extrapolated to the full phase space over $p_T$ and $\eta_{\text{lab}}$ by the acceptance correction. Each component of Eq. (2) is presented and systematic uncertainties summarized below.

3.1 Signal and background

The $Z$ candidate events are selected by requiring a same-flavor, oppositely-charged lepton pair with an invariant mass in the 60–120$\text{ GeV}/c^2$ range, where both leptons satisfy the acceptance and quality requirements and at least one of them corresponds to the lepton that triggered the event. Figure 1 shows the invariant mass distribution of the selected lepton pairs compared to a combination of PYTHIA 6 and HIJING (PYTHIA 6+HIJING) Monte Carlo (MC) simulations. The $pN \rightarrow Z \rightarrow \ell\ell$ process is simulated using the PYTHIA 6 generator (version 6.424, tune Z2 [32]) with a mixture of pp and pn interactions corresponding to pPb collisions. Each PYTHIA 6 signal event is embedded in a minimum bias pPb background event which is produced with the HIJING event generator version 1.383 [33]. The detector response for each produced event is simulated with GEANT4 [34]. The signal and background events have the same generated vertex location and are boosted to have the correct rapidity distribution in the laboratory frame. The embedding is done at the level of detector hits and then the events are processed through the trigger emulation and the event reconstruction chains. The reconstructed longitudinal primary vertex and overall multiplicity distributions are reweighted to match those observed in data.

An electron energy scale correction is extracted by fitting the energy to momentum ratio of electrons in a very pure $W \rightarrow e\nu$ control sample [29]. After fixing the shape of the distribution from MC, the energy to momentum ratio in data is fitted to derive the difference of the energy scale between data and MC, and then the data is corrected for this difference. A correction of the electron energy resolution is applied to MC by comparing the mass distribution of electron pairs between data and MC. Such corrections are also estimated for the $Z \rightarrow \mu^+\mu^-$ channel and found to be negligible.

The raw yield, $S$, of $Z$ boson candidates in the pPb sample is determined by counting the number of oppositely-charged lepton pairs in the 60–120$\text{ GeV}/c^2$ mass region that fulfill the acceptance and quality requirements. This number is found to be 2183 in the muon channel and 1571 in the electron channel. The difference between the two channels is due to the tighter selection criteria applied to the electrons in order to suppress the higher background. A charge
misidentification correction of 1% is applied to the dielectron yields; this correction is negligible for dimuons. No events are found with more than one Z boson candidate. For the differential cross sections, the measurement is performed in the dilepton transverse momentum or rapidity bins, where the rapidity is calculated in the center-of-mass frame.

Possible background contributions to the $Z \rightarrow \ell\ell$ production are QCD multijet events, $t\bar{t}$ pairs and electroweak processes such as $W$+jets, diboson ($WW$, $WZ$, $ZZ$), and $Z \rightarrow \tau\tau$ production. Although the expected background contamination is small, an estimate based on data is used to subtract its contribution from the dilepton raw yield. For $t\bar{t}$, $b\bar{b}$, $WW$, and $Z \rightarrow \tau\tau$ processes, two electron-muon events are expected for each dimuon or dielectron event, because of lepton universality. In the Z boson mass range, the oppositely-charged electron-muon pairs are counted and translated into the expected number of muon or electron pairs, taking into account the differences in the muon and electron reconstruction and selection efficiencies. This background is subtracted from the dilepton raw yield and accounts for the main electroweak and $t\bar{t}$ backgrounds, as well as for the part of QCD multijet background (such as $b\bar{b}$ decays) that produces oppositely-charged leptons. The background from random combinations of other leptons in the event is estimated by counting the same-charge pairs. Additional electroweak contributions from $W$+jets and diboson production are found to be negligible via MC simulations. The fraction of background events subtracted from the raw yield is 2.4% (2.9%) in the muon (electron) channel, where the dominant background contribution comes from QCD processes, since no isolation requirements are imposed on the leptons.

### 3.2 Efficiency and acceptance

The efficiency, $\epsilon$, for Z bosons is defined as the number of reconstructed Z candidates, where both leptons fulfill the acceptance and quality requirements, divided by the number of generated Z bosons where both leptons fulfill the acceptance requirements. This combined reconstruction, lepton identification, and trigger efficiency is calculated from the PYTHIA 6+HIJING simulation samples so that the effects of the pPb environment are taken into account.

For the rapidly falling dilepton $p_T$ spectrum, an unfolding technique based on the inversion of a response matrix similar to the one used in Ref. [4] is first applied to the data before applying the
efficiency correction. The response matrix is constructed from the PYTHIA 6+HIJING simulation to take into account the detector resolution effects. The dilepton $p_T$ resolution is about 0.5–1.5 GeV/$c$, which results in a maximum bin-to-bin spill of about 30% in the lowest $p_T$ bins chosen for this analysis. In the measurement of the dilepton rapidity, the unfolding is not necessary as the shape of the $y_{cm}$ spectrum is almost flat and the resolution is a small fraction of the analysis bin size. Instead, the resolution effects in rapidity are taken into account in the efficiency corrections.

In order to correct for possible differences between data and simulation, a method derived from data is used to determine correction factors to the baseline efficiency from simulation. These correction factors are determined as a function of lepton $\eta$ and $p_T$ by applying the tag-and-probe method to both data and simulation to calculate single lepton efficiencies for reconstruction, identification, and triggering, similar to the method described in Ref. [28]. The ratio of each efficiency from data over the corresponding efficiency in the simulation is then applied to reweight the simulation on a lepton-by-lepton basis. The efficiency for the Z bosons, after correcting for the small differences between data and simulation, is found to be $0.878 \pm 0.015$ in the dimuon and $0.605 \pm 0.015$ in the dielectron decay channel. The sources of systematic uncertainties are described in Section 3.3.

The acceptance, $\alpha$, is defined as the number of generated dilepton events where both leptons fulfill the acceptance requirements ($p_T^\ell > 20\text{ GeV}/c$, $|\eta^\ell_{\text{lab}}| < 2.4$) divided by the number of all generated dilepton events in the 60–120 GeV/$c^2$ mass range. It is calculated using simulated events. The event generation is provided by the POWHEG generator [35–38] with the CT10 free proton PDF set [39], interfaced with PYTHIA 6 parton shower, and the events are boosted to the laboratory frame (POWHEG+PYTHIA 6). Final-state photon radiation is also simulated by PYTHIA 6. The integrated acceptance is found to be $0.516 \pm 0.026$ in both decay channels.

### 3.3 Systematic uncertainties

The total systematic uncertainty in the Z boson production cross section is calculated by adding in quadrature the different contributions from the background subtraction, acceptance and efficiency determination, and the unfolding technique. The integrated luminosity, calibrated by the van der Meer scans [27], has a systematic uncertainty of 3.5%. It is the dominant systematic uncertainty of the measurement in the fiducial region.

The signal yield of Z candidates is affected by the uncertainty in the background subtraction method. The number of subtracted background events determined by the electron-muon method is varied conservatively by $\pm 100\%$ to assign an uncertainty in the signal yield. The uncertainty in the signal yield from this background variation is 1.7% (1.8%) in the muon (electron) channel.

The uncertainty in the correction factor for the electron energy scale is propagated as a systematic uncertainty in the dielectron yield. It is estimated to be 0.5% in the inclusive yield and varies across the analysis $p_T$ bins between 4 and 19%. The residual difference in the mass resolution between data and simulation is taken as the systematic uncertainty in the electron channel. After propagating to the inclusive cross section, it accounts for a 1.1% uncertainty.

The systematic uncertainty in the efficiency comes from two different sources. The first one is the uncertainty in the underlying rapidity and transverse momentum distributions reflecting the poorly known PDFs. This is estimated by applying a weight to the generated events that varies linearly between 0.7 and 1.3 over the $-3 < y_{cm} < 3$ range, and a weight that varies between 0.9 and 1.1 over the $0 < p_T < 150\text{ GeV}/c$ range. These variations cover the predicted
Results

nuclear effects to the rapidity and $p_T$ spectrum from different groups \cite{21, 22, 24} as well as the statistical uncertainties in the present measurement and result in a 0.2\% uncertainty in the dilepton efficiency. Second, the statistical uncertainty in the correction factors coming from the ratio of data and simulation in the tag-and-probe method is propagated to the dilepton efficiency. In addition, the tag-and-probe technique itself carries an uncertainty of about 1\%, estimated from differences observed in the efficiencies by varying the functional form or the range of the fits. Finally, the uncertainties in the three different components of the efficiency are combined in quadrature, resulting in an overall uncertainty in the dimuon (dielectron) efficiency of 1.7\% (2.5\%).

All the uncertainties above are evaluated in bins of dilepton rapidity and transverse momentum to give uncertainties in the differential cross sections. The systematic uncertainty of the forward-backward asymmetry is calculated from the rapidity differential cross section. The uncertainties in the background, electron energy scale, and efficiency are propagated without assuming any cancellation. The uncertainty of the luminosity cancels in the ratio.

There is an additional uncertainty in the dilepton $p_T$ spectrum coming from the matrix inversion procedure used for the unfolding. This uncertainty is determined by varying the generated dilepton $p_T$ distribution and the single lepton $p_T$ resolution. The reconstructed $p_T$ distributions from PYTHIA 6+HIJING and POWHEG+PYTHIA 6, as well as the weighted $p_T$ spectrum reflecting possible nPDF differences, are all studied and their effect on the results is directly evaluated. These two sources give a combined uncertainty in the unfolded yield of about 1–5\%, depending on the $p_T$ bin.

The uncertainty due to the acceptance correction is estimated by changing the shape of the generated rapidity and $p_T$ distributions of the Z bosons with the same functions as described for the efficiency uncertainty in order to cover differences in PDFs and possible nuclear effects. The resulting uncertainty in the acceptance is about 5\% from the extrapolation to the most forward and backward rapidity regions and it only affects the total cross section. Table 1 summarizes the systematic uncertainties in the two decay channels.

<table>
<thead>
<tr>
<th>Source</th>
<th>$Z \rightarrow \mu\mu$</th>
<th>$Z \rightarrow ee$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Background</td>
<td>1.7%</td>
<td>1.8%</td>
</tr>
<tr>
<td>Electron energy scale</td>
<td>—</td>
<td>0.5%</td>
</tr>
<tr>
<td>Electron resolution</td>
<td>—</td>
<td>1.1%</td>
</tr>
<tr>
<td>Efficiency</td>
<td>1.7%</td>
<td>2.5%</td>
</tr>
<tr>
<td>Unfolding of $p_T$ spectrum</td>
<td>1–5%</td>
<td></td>
</tr>
<tr>
<td>Acceptance</td>
<td>5%</td>
<td></td>
</tr>
<tr>
<td>Luminosity</td>
<td>3.5%</td>
<td></td>
</tr>
<tr>
<td>Total (fiducial cross section)</td>
<td>4.2%</td>
<td>4.8%</td>
</tr>
<tr>
<td>Total (total cross section)</td>
<td>6.6%</td>
<td>6.9%</td>
</tr>
</tbody>
</table>

4 Results

The results are primarily compared to the NLO pp predictions from the POWHEG+PYTHIA 6 generator using the CT10 \cite{39} free proton PDF set. The pN $\rightarrow Z \rightarrow \ell\ell$ process is also simulated with the MCFM \cite{40} generator (version 6.7) using the CT10 free proton PDF set, as well as the EPS09 \cite{14} and DSSZ \cite{13} nuclear PDF sets. Since these predictions include theoretical uncertainties, their statistical compatibility with the measurements can be tested. All predictions are
scaled by the number of nucleons in the Pb nucleus ($A = 208$) as is expected in the case of elementary nucleon-nucleon collision scaling.

The cross section of $Z$ boson production is calculated using Eq. (2) for both decay channels. The analysis of the muon channel results in a fiducial cross section ($p_T^\ell > 20$ GeV/$c$, $|\eta^\ell_{\text{lab}}| < 2.4$) of $70.1 \pm 1.5$ (stat) $\pm 1.7$ (syst) $\pm 2.5$ (lumi) nb and the electron channel gives $73.9 \pm 1.9$ (stat) $\pm 2.8$ (syst) $\pm 2.6$ (lumi) nb.

The muon and electron results, which agree within statistical and systematic uncertainties, are combined, separating out the uncertainty related to the integrated luminosity. The best linear unbiased estimate (BLUE) technique [41] is applied, taking the muon and electron channel cross sections and their uncertainties in each bin to be uncorrelated.

The measured inclusive $Z$ boson production cross section in the fiducial region, where both leptons fulfill the acceptance requirements is

$$\sigma_{p\text{Pb} \to Z \to \ell\ell}(p_T^\ell > 20 \text{ GeV}/c, |\eta^\ell_{\text{lab}}| < 2.4) = 71.3 \pm 1.2 \text{ (stat)} \pm 1.5 \text{ (syst)} \pm 2.5 \text{ (lumi)} \text{ nb.}$$

(3)

The $\text{POWHEG}+\text{PYTHIA}$ 6 prediction gives a $Z$ boson cross section in $pp$ collisions at $\sqrt{s} = 5.02$ TeV of $338 \pm 17$ pb for $Z \to \ell\ell$ production in the $60–120 \text{ GeV}/c^2$ mass range after applying the acceptance requirements on the leptons. The uncertainties in the theoretical prediction in $pp$ collisions amount to about 5% and arise from missing higher-order corrections and from the uncertainties in the PDF sets. Scaling the pp cross section by $A = 208$, results in the prediction of $70.4 \pm 3.5$ nb for the $p\text{Pb}$ cross section, which is consistent with the measured value.

For the acceptance-corrected total cross section, the systematic uncertainty in the acceptance is correlated between the two decay channels, which is taken into account in the BLUE method. The combined total $Z$ boson production cross section in the $60–120 \text{ GeV}/c^2$ mass region is

$$\sigma_{p\text{Pb} \to Z \to \ell\ell} = 138.1 \pm 2.4 \text{ (stat)} \pm 8.6 \text{ (syst)} \pm 4.8 \text{ (lumi)} \text{ nb.}$$

(4)

This measurement has an uncertainty of about 5% from the extrapolation of the detector acceptance to the full phase space. The $\text{POWHEG}+\text{PYTHIA}$ 6 generator after scaling predicts $136.1 \pm 6.8$ nb, which is consistent with the measured value.

Figure 2 shows the differential cross section of the $Z$ bosons in the fiducial region in $p\text{Pb}$ collisions as a function of rapidity. The luminosity normalization uncertainty of 3.5% is not shown. The MCFM theoretical predictions, both with and without nuclear modification, are consistent with the measured differential cross section within uncertainties. The corresponding rapidity dependence predicted by $\text{POWHEG}+\text{PYTHIA}$ 6 for $pp$ collisions agrees with the MCFM calculation for $pN$ collisions using the CT10 PDF set without nuclear modification, showing that any dependences on isospin or the PDF set are within the theoretical uncertainties.

Nuclear effects are expected to modify the rapidity distribution asymmetrically and thus they can be further quantified by the forward-backward asymmetry defined in Eq. (1). This quantity is expected to be more sensitive to nuclear effects [24] because normalization uncertainties cancel both in theory and in experiment. Figure 3 shows the measured forward-backward asymmetry as a function of $|y_{\text{cm}}|$ compared to the MCFM predictions with and without nuclear modification.

While being consistent with the three theoretical predictions shown, the data tend to favor the presence of nuclear effects in PDFs. The ATLAS collaboration reached similar conclusions from their $Z$ boson measurement [19]. Together with the measured $W$ boson production in $p\text{Pb}$ collisions [17], these results can reduce the nPDF uncertainties by adding new data to the global fits in a previously unexplored region of the $(Q^2, x)$ phase space.
Figure 2: Differential cross section of the Z bosons in pPb collisions as a function of rapidity in the fiducial region for the combined leptonic decay channel. Colored boxes are predictions from the MCFM generator, scaled by 208 (see text), and using nuclear (EPS09 and DSSZ) or free (CT10) PDF sets. The bottom panel shows the ratio of the data and the nPDF predictions to the CT10 PDF set. The vertical bars (boxes) represent the statistical (systematic) uncertainties.

In order to quantify the agreement between the measurements and the predictions with the different PDF sets, a $\chi^2$ test is performed for the rapidity-dependent differential cross section and the forward-backward asymmetry. The few correlations in the experimental uncertainties, only relevant for the cross section but not for the asymmetry, are taken into account, as well as the correlations in the theoretical uncertainties. The resulting $\chi^2$ values and probabilities are given in Table 2. The theoretical calculations including nuclear effects provide a somewhat better description of the measurements.

Table 2: Results of the $\chi^2$ test between the measurements and the theoretical predictions with and without nuclear modification from the EPS09 or DSSZ nPDF sets. The differential cross section and the forward-backward asymmetry have twelve and five numbers of degrees of freedom (NDF), respectively.

<table>
<thead>
<tr>
<th>Observable</th>
<th>CT10</th>
<th>CT10+EPS09</th>
<th>CT10+DSSZ</th>
</tr>
</thead>
<tbody>
<tr>
<td>$d\sigma/dy_{cm}$</td>
<td>$\chi^2$/NDF</td>
<td>Probability</td>
<td>$\chi^2$/NDF</td>
</tr>
<tr>
<td>$d\sigma/dy_{cm}$</td>
<td>10.8/12</td>
<td>54%</td>
<td>7.4/12</td>
</tr>
<tr>
<td>$R_{FB}$</td>
<td>7.3/5</td>
<td>20%</td>
<td>3.9/5</td>
</tr>
</tbody>
</table>

Figure 4 shows the differential cross section as a function of $p_T$ in the fiducial region. The results are compared only to theoretical predictions from POWHEG+PYTHIA 6, because the expected nuclear modification of the $p_T$ spectrum is small compared to the uncertainties in the theory [21, 22]. No large deviations are found from the theoretical cross sections, apart from the lowest dilepton $p_T$ bins where the differences from POWHEG+PYTHIA 6 are similar to the ones observed in the pp measurements at 7 TeV [2, 4].

5 Summary

The cross section of Z boson production has been measured in the muon and electron decay channels in pPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The NLO pp inclusive cross section from
Figure 3: Forward-backward asymmetry $R_{FB}$ distribution of the Z bosons in pPb collisions as a function of rapidity in the fiducial region for the combined leptonic decay channel compared to the predictions from the MCFM generator with nuclear (EPS09 and DSSZ) or free (CT10) PDF sets. The bottom panel shows the ratio of the data and the nPDF predictions to the CT10 PDF set. The vertical bars (boxes) represent the statistical (systematic) uncertainties.

POWHEG+PYTHIA 6 scaled by the number of elementary nucleon-nucleon collisions is in agreement with the measured pPb cross section. The pPb theoretical predictions for the differential cross section as a function of the Z boson rapidity with and without nuclear effects are compared to the measurement. Given the small differences in these predictions and their inherent theoretical uncertainties as well as the sensitivity of the data, both scenarios, presence or not of nuclear effects, are consistent with the data. A more sensitive variable, the forward-backward asymmetry, deviates from predictions assuming free proton PDFs by an amount which is compatible with both the EPS09 and the DSSZ nPDF modifications, although the statistical precision of the measurement precludes making a definitive statement. The differential cross section as a function of the Z boson transverse momentum has been measured and is found to be in agreement with pp predictions from POWHEG+PYTHIA 6, except at very low transverse momentum, where similar deviations as previously seen in pp are observed. The presented results provide new data for constraining nuclear PDF fits.

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Figure 4: Differential cross section of the Z bosons in pPb collisions as a function of transverse momentum in the fiducial region for the combined leptonic decay channel compared to the prediction from the POWHEG+PYTHIA 6 generator scaled by the number of nucleons in the Pb nucleus. The vertical bars (boxes) represent the statistical (systematic) uncertainties. The 3.5% luminosity uncertainty is shown in the ratio plot as a hashed band together with the assumed 5% theoretical uncertainty, shown as a yellow band.

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References


References


A The CMS Collaboration

Yerevan Physics Institute, Yerevan, Armenia
V. Khachatryan, A.M. Sirunyan, A. Tumasyan

Institut für Hochenergiephysik der OeAW, Wien, Austria

National Centre for Particle and High Energy Physics, Minsk, Belarus
V. Mossolov, N. Shumeiko, J. Suarez Gonzalez

Universiteit Antwerpen, Antwerpen, Belgium

Vrije Universiteit Brussel, Brussel, Belgium

Université Libre de Bruxelles, Bruxelles, Belgium

Ghent University, Ghent, Belgium

Université Catholique de Louvain, Louvain-la-Neuve, Belgium

Université de Mons, Mons, Belgium
N. Beliy, G.H. Hammad

Centro Brasileiro de Pesquisas Fisicas, Rio de Janeiro, Brazil

Universidade do Estado do Rio de Janeiro, Rio de Janeiro, Brazil
Universidade Estadual Paulista \textsuperscript{a}, Universidade Federal do ABC \textsuperscript{b}, São Paulo, Brazil
S. Ahuja\textsuperscript{a}, C.A. Bernardes\textsuperscript{b}, A. De Souza Santos\textsuperscript{b}, S. Dogra\textsuperscript{a}, T.R. Fernandez Perez Tomei\textsuperscript{a}, E.M. Gregores\textsuperscript{b}, P.G. Mercadante\textsuperscript{b}, C.S. Moon\textsuperscript{a,7}, S.F. Novaes\textsuperscript{a}, Sandra S. Padula\textsuperscript{a}, D. Romero Abad\textsuperscript{b}, J.C. Ruiz Vargas

Institute for Nuclear Research and Nuclear Energy, Sofia, Bulgaria
A. Aleksandrov, R. Hadjiiska, P. Iaydjiev, M. Rodozov, S. Stoykova, G. Sultanov, M. Vutova

University of Sofia, Sofia, Bulgaria
A. Dimitrov, I. Glushkov, L. Litov, B. Pavlov, P. Petkov

Institute of High Energy Physics, Beijing, China

State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing, China
C. Asawatangtrakuldee, Y. Ban, Q. Li, S. Liu, Y. Mao, S.J. Qian, D. Wang, Z. Xu

Universidad de Los Andes, Bogota, Colombia
C. Avila, A. Cabrera, L.F. Chaparro Sierra, C. Florez, J.P. Gomez, B. Gomez Moreno, J.C. Sanabria

University of Split, Faculty of Electrical Engineering, Mechanical Engineering and Naval Architecture, Split, Croatia
N. Godinovic, D. Lelas, I. Puljak, P.M. Ribeiro Cipriano

University of Split, Faculty of Science, Split, Croatia
Z. Antunovic, M. Kovac

Institute Rudjer Boskovic, Zagreb, Croatia
V. Brigljevic, K. Kadija, J. Luetic, S. Micanovic, L. Sudic

University of Cyprus, Nicosia, Cyprus

Charles University, Prague, Czech Republic
M. Bodlak, M. Finger\textsuperscript{9}, M. Finger Jr.\textsuperscript{9}

Academy of Scientific Research and Technology of the Arab Republic of Egypt, Egyptian Network of High Energy Physics, Cairo, Egypt
E. El-khateeb\textsuperscript{10,10}, T. Elkafrawy\textsuperscript{10}, A. Mohamed\textsuperscript{11}, E. Salama\textsuperscript{12,10}

National Institute of Chemical Physics and Biophysics, Tallinn, Estonia
B. Calpas, M. Kadastik, M. Murumaa, M. Raidal, A. Tiko, C. Veelken

Department of Physics, University of Helsinki, Helsinki, Finland
P. Eerola, J. Pekkanen, M. Voutilainen

Helsinki Institute of Physics, Helsinki, Finland
J. Härkönen, V. Karimäki, R. Kinnunen, T. Lampén, K. Lassila-Perini, S. Lehti, T. Lindén, P. Luukka, T. Peltola, J. Tuominiemi, E. Tuovinen, L. Wendland

Lappeenranta University of Technology, Lappeenranta, Finland
J. Talvitie, T. Tuuva

DSM/IRFU, CEA/Saclay, Gif-sur-Yvette, France
M. Besancon, F. Coudenc, M. Dejardin, D. Denegri, B. Fabbro, J.L. Faure, C. Favaro, F. Ferri,

University of Hamburg, Hamburg, Germany

Institut für Experimentelle Kernphysik, Karlsruhe, Germany

Institute of Nuclear and Particle Physics (INPP), NCSR Demokritos, Aghia Paraskevi, Greece

National and Kapodistrian University of Athens, Athens, Greece
A. Agapitos, S. Kesisoglou, A. Panagiotou, N. Saoulidou, E. Tziaferi

University of Ioánnina, Ioánnina, Greece

Wigner Research Centre for Physics, Budapest, Hungary

Institute of Nuclear Research ATOMKI, Debrecen, Hungary
N. Beni, S. Czellar, J. Karancsi²⁰, J. Molnar, Z. Szillasi²

University of Debrecen, Debrecen, Hungary
M. Bartók²¹, A. Makovec, P. Raics, Z.L. Trocsanyi, B. Ujvari

National Institute of Science Education and Research, Bhubaneswar, India

Panjab University, Chandigarh, India

University of Delhi, Delhi, India
Ashok Kumar, A. Bhardwaj, B.C. Choudhary, R.B. Garg, S. Malhotra, M. Naimuddin, N. Nishu, K. Ranjan, R. Sharma, V. Sharma
Saha Institute of Nuclear Physics, Kolkata, India

Bhabha Atomic Research Centre, Mumbai, India
R. Chudasama, D. Dutta, V. Jha, V. Kumar, A.K. Mohanty, L.M. Pant, P. Shukla, A. Topkar

Tata Institute of Fundamental Research, Mumbai, India

Indian Institute of Science Education and Research (IISER), Pune, India
S. Chauhan, S. Dube, A. Kapoor, K. Kothekar, S. Sharma

Institute for Research in Fundamental Sciences (IPM), Tehran, Iran
H. Bakhshiansohi, H. Behnamian, S.M. Etamian, F. Fahim, M. Khakzad, M. Mohammad Najafabadi, M. Naseri, S. Paktinat Mehdiabadi, F. Rezaei Hosseinabadi, B. Safarzadeh, Z. Zainali

University College Dublin, Dublin, Ireland
M. Felcini, M. Grunewald

INFN Sezione di Bari, Università di Bari, Politecnico di Bari, Bari, Italy

INFN Sezione di Bologna, Università di Bologna, Bologna, Italy

INFN Sezione di Catania, Università di Catania, Catania, Italy
G. Cappello, M. Chiorboli, S. Costa, A. Di Mattia, F. Giordano, R. Potenza, A. Tricomi, C. Tuve

INFN Sezione di Firenze, Università di Firenze, Firenze, Italy
G. Barbaglio, V. Ciulli, C. Cividini, R. D’Alessandro, E. Focardi, V. Gori, P. Lenzi, M. Meschini, S. Paolelli, G. Sguazzoni, L. Viliani

INFN Laboratori Nazionali di Frascati, Frascati, Italy
L. Benussi, S. Bianco, F. Fabbr, D. Piccolo, F. Primavera

INFN Sezione di Genova, Università di Genova, Genova, Italy
V. Calvelli, F. Ferro, M. Lo Vetere, M.R. Monge, E. Robutti, S. Tosi

INFN Sezione di Milano-Bicocca, Università di Milano-Bicocca, Milano, Italy
Chonnam National University, Institute for Universe and Elementary Particles, Kwangju, Korea
S. Song

Korea University, Seoul, Korea

Seoul National University, Seoul, Korea
H.D. Yoo

University of Seoul, Seoul, Korea

Sungkyunkwan University, Suwon, Korea
Y. Choi, J. Goh, D. Kim, E. Kwon, J. Lee, I. Yu

Vilnius University, Vilnius, Lithuania
V. Dudenas, A. Juodagalvis, J. Vaitkus

National Centre for Particle Physics, Universiti Malaya, Kuala Lumpur, Malaysia

Centro de Investigacion y de Estudios Avanzados del IPN, Mexico City, Mexico

Universidad Iberoamericana, Mexico City, Mexico
S. Carrillo Moreno, F. Vazquez Valencia

Benemerita Universidad Autonoma de Puebla, Puebla, Mexico
I. Pedraza, H.A. Salazar Ibarguen

Universidad Autónoma de San Luis Potosí, San Luis Potosí, Mexico
A. Morelos Pineda

University of Auckland, Auckland, New Zealand
D. Krofcheck

University of Canterbury, Christchurch, New Zealand
P.H. Butler

National Centre for Physics, Quaid-I-Azam University, Islamabad, Pakistan
A. Ahmad, M. Ahmad, Q. Hassan, H.R. Hoorani, W.A. Khan, T. Khurshid, M. Shoaib, M. Waqas

National Centre for Nuclear Research, Swierk, Poland

Institute of Experimental Physics, Faculty of Physics, University of Warsaw, Warsaw, Poland
G. Brona, K. Bunkowski, A. Byyszuk34, K. Doroba, A. Kalinowski, M. Konecki, J. Krollikowski, M. Misjura, M. Olszewski, M. Walczak

Laboratório de Instrumentação e Física Experimental de Partículas, Lisboa, Portugal
P. Bargassa, C. Beirão Da Cruz E Silva, A. Di Francesco, P. Faccioli, P.G. Ferreira Parracho,
Chulalongkorn University, Faculty of Science, Department of Physics, Bangkok, Thailand
B. Asavapibhop, K. Kovitanggoon, G. Singh, N. Srimanobhas, N. Suwonjandee

Cukurova University, Adana, Turkey

Middle East Technical University, Physics Department, Ankara, Turkey
B. Bilin, S. Bilmis, B. Isildak, G. Karapinar, M. Yalvac, M. Zeyrek

Bogazici University, Istanbul, Turkey
E. Gülmez, M. Kaya, O. Kaya, E.A. Yetkin, T. Yetkin

Istanbul Technical University, Istanbul, Turkey
A. Cakir, K. Cankocak, S. Sen, F.I. Vardarlı

Institute for Scintillation Materials of National Academy of Science of Ukraine, Kharkov, Ukraine
B. Grynyov

National Scientific Center, Kharkov Institute of Physics and Technology, Kharkov, Ukraine
L. Levchuk, P. Sorokin

University of Bristol, Bristol, United Kingdom

Rutherford Appleton Laboratory, Didcot, United Kingdom

Imperial College, London, United Kingdom

Brunel University, Uxbridge, United Kingdom
J.E. Cole, P.R. Hobson, A. Khan, P. Kyberd, D. Leslie, I.D. Reid, P. Symonds, L. Teodorescu, M. Turner

Baylor University, Waco, USA
A. Borzou, K. Call, J. Dittmann, K. Hatakeyama, H. Liu, N. Pastika

The University of Alabama, Tuscaloosa, USA
O. Charaf, S.I. Cooper, C. Henderson, P. Rumerio

Boston University, Boston, USA
D. Arcaro, A. Avetisyan, T. Bose, D. Gastler, D. Rankin, C. Richardson, J. Rohlf, L. Sulak, D. Zou
Brown University, Providence, USA

University of California, Davis, Davis, USA

University of California, Los Angeles, USA

University of California, Riverside, Riverside, USA

University of California, San Diego, La Jolla, USA

University of California, Santa Barbara, Santa Barbara, USA

California Institute of Technology, Pasadena, USA

Carnegie Mellon University, Pittsburgh, USA

University of Colorado Boulder, Boulder, USA

Cornell University, Ithaca, USA

Fermi National Accelerator Laboratory, Batavia, USA

University of Florida, Gainesville, USA

Florida International University, Miami, USA
S. Hewamanage, S. Linn, P. Markowitz, G. Martinez, J.L. Rodriguez

Florida State University, Tallahassee, USA

Florida Institute of Technology, Melbourne, USA

University of Illinois at Chicago (UIC), Chicago, USA

The University of Iowa, Iowa City, USA

Johns Hopkins University, Baltimore, USA

The University of Kansas, Lawrence, USA

Kansas State University, Manhattan, USA
A. Ivanov, K. Kaadze, S. Khalil, M. Makouski, Y. Maravin, A. Mohammadi, L.K. Saini, N. Skhirtladze, S. Toda

Lawrence Livermore National Laboratory, Livermore, USA
D. Lange, F. Rebassoo, D. Wright

University of Maryland, College Park, USA

Massachusetts Institute of Technology, Cambridge, USA
Rice University, Houston, USA

University of Rochester, Rochester, USA
B. Betchart, A. Bodek, P. de Barbaro, R. Demina, Y. Eshaq, T. Ferbel, M. Galanti, A. Garcia-Bellido, J. Han, O. Hindrichs, A. Khukhunaishvili, K.H. Lo, P. Tan, M. Verzetti

Rutgers, The State University of New Jersey, Piscataway, USA

University of Tennessee, Knoxville, USA
M. Foerster, G. Riley, K. Rose, S. Spanier, K. Thapa

Texas A&M University, College Station, USA

Texas Tech University, Lubbock, USA

Vanderbilt University, Nashville, USA

University of Virginia, Charlottesville, USA

Wayne State University, Detroit, USA
C. Clarke, R. Harr, P.E. Karchin, C. Kottachchi Kankanamge Don, P. Lamichhane, J. Sturdy

University of Wisconsin - Madison, Madison, WI, USA

†: Deceased
1: Also at Vienna University of Technology, Vienna, Austria
2: Also at CERN, European Organization for Nuclear Research, Geneva, Switzerland
3: Also at State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing, China
4: Also at Institut Pluridisciplinaire Hubert Curien, Université de Strasbourg, Université de Haute Alsace Mulhouse, CNRS/IN2P3, Strasbourg, France
5: Also at Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, Moscow, Russia
6: Also at Universidade Estadual de Campinas, Campinas, Brazil
7: Also at Centre National de la Recherche Scientifique (CNRS) - IN2P3, Paris, France
8: Also at Laboratoire Leprince-Ringuet, Ecole Polytechnique, IN2P3-CNRS, Palaiseau, France
9: Also at Joint Institute for Nuclear Research, Dubna, Russia
10: Also at Ain Shams University, Cairo, Egypt
11: Also at Zewail City of Science and Technology, Zewail, Egypt
12: Also at British University in Egypt, Cairo, Egypt
13: Also at Université de Haute Alsace, Mulhouse, France
14: Also at Tbilisi State University, Tbilisi, Georgia
15: Also at RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany
16: Also at University of Hamburg, Hamburg, Germany
17: Also at Brandenburg University of Technology, Cottbus, Germany
18: Also at Institute of Nuclear Research ATOMKI, Debrecen, Hungary
19: Also at Eötvös Loránd University, Budapest, Hungary
20: Also at University of Debrecen, Debrecen, Hungary
21: Also at Wigner Research Centre for Physics, Budapest, Hungary
22: Also at Indian Institute of Science Education and Research, Bhopal, India
23: Also at University of Visva-Bharati, Santiniketan, India
24: Now at King Abdulaziz University, Jeddah, Saudi Arabia
25: Also at University of Ruhuna, Matara, Sri Lanka
26: Also at Isfahan University of Technology, Isfahan, Iran
27: Also at University of Tehran, Department of Engineering Science, Tehran, Iran
28: Also at Plasma Physics Research Center, Science and Research Branch, Islamic Azad University, Tehran, Iran
29: Also at Università degli Studi di Siena, Siena, Italy
30: Also at Purdue University, West Lafayette, USA
31: Also at International Islamic University of Malaysia, Kuala Lumpur, Malaysia
32: Also at Malaysian Nuclear Agency, MOSTI, Kajang, Malaysia
33: Also at Consejo Nacional de Ciencia y Tecnología, Mexico city, Mexico
34: Also at Warsaw University of Technology, Institute of Electronic Systems, Warsaw, Poland
35: Also at University of Debrecen, Debrecen, Hungary
36: Also at INFN Sezione di Padova; Università di Padova; Università di Trento (Trento), Padova, Italy
37: Also at INFN Sezione di Roma; Università di Roma, Roma, Italy
38: Also at Scuola Normale e Sezione dell’INFN, Pisa, Italy
39: Also at National Technical University of Athens, Athens, Greece
40: Also at Faculty of Physics, University of Belgrade, Belgrade, Serbia
41: Also at INFN Sezione di Roma; Università di Roma, Roma, Italy
42: Also at National Technical University of Athens, Athens, Greece
43: Also at Albert Einstein Center for Fundamental Physics, Bern, Switzerland
44: Also at Institute for Theoretical and Experimental Physics, Moscow, Russia
45: Also at Piri Reis University, Adiyaman, Turkey
46: Also at Adiyaman University, Adiyaman, Turkey
47: Also at Mersin University, Mersin, Turkey
48: Also at Cag University, Mersin, Turkey
49: Also at Piri Reis University, Istanbul, Turkey
50: Also at Gaziosmanpasa University, Tokat, Turkey
51: Also at Ozyegin University, Istanbul, Turkey
52: Also at Izmir Institute of Technology, Izmir, Turkey
53: Also at Marmara University, Istanbul, Turkey
54: Also at Kafkas University, Kars, Turkey
55: Also at Istanbul Bilgi University, Istanbul, Turkey
56: Also at Yildiz Technical University, Istanbul, Turkey
57: Also at Hacettepe University, Ankara, Turkey
58: Also at Rutherford Appleton Laboratory, Didcot, United Kingdom
59: Also at School of Physics and Astronomy, University of Southampton, Southampton, United Kingdom
60: Also at Instituto de Astrofísica de Canarias, La Laguna, Spain
61: Also at Utah Valley University, Orem, USA
62: Also at University of Belgrade, Faculty of Physics and Vinca Institute of Nuclear Sciences, Belgrade, Serbia
63: Also at Facoltà Ingegneria, Università di Roma, Roma, Italy
64: Also at Argonne National Laboratory, Argonne, USA
65: Also at Erzincan University, Erzincan, Turkey
66: Also at Mimar Sinan University, Istanbul, Istanbul, Turkey
67: Also at Texas A&M University at Qatar, Doha, Qatar
68: Also at Kyungpook National University, Daegu, Korea